Fasc.: 3-4 Year: 2019 Vol.: 95

Title: Rings in which every element is the sum of a left zero-divisor and an idempotent

Author(s): Ebrahim Ghashghaei and Muhammet Tamer Koşan

A ring R is called *left zero-clean* if every element is the sum of a left zero-divisor and an idempotent. This class of rings is a natural generalization of O-rings and nil-clean rings. We determine when a skew polynomial ring is a left zero-clean ring. It is proved that a ring R is left zero-clean if and only if the upper triangular matrix ring $\mathbb{T}_n(R)$ is left zero-clean. It is shown that a commutative ring R is zero-clean if and only if the matrix ring $\mathbb{M}_n(R)$ is zero-clean for every positive integer $n \geq 1$. We characterize the zero-clean matrix rings over fields. We also determine when a 2×2 matrix A over a field is left zero-clean. A ring is called *uniquely left zeroclean* if every element is uniquely the sum of a left zero-divisor and an idempotent. We completely determine when a ring is uniquely left zero-clean.

Address:

Ebrahim Ghashghaei Department of Mathematics Shahid Chamran University of Ahvaz Ahvaz Iran Address:

Muhammet Tamer Koşan Department of Mathematics Faculty of Sciences Gazi University Ankara Turkey