Let $H$ and $T$ be subgroups of a group $G$. Then we call $H$ conditionally permutable (or in brevity, $c$-permutable) with $T$ in $G$ if there exists an element $x \in G$ such that $HT^x = T^xH$. If $H$ is $c$-permutable with $T$ in $\langle H, T \rangle$, then we call $H$ completely $c$-permutable with $T$ in $G$. By using the above concepts, we will give some new criterions for the supersolubility of a finite group $G = AB$, where $A$ and $B$ are both supersoluble groups. In particular, we prove that a finite group $G$ is supersoluble if and only if $G = AB$, where both $A, B$ are nilpotent subgroups of the group $G$ and $B$ is completely $c$-permutable in $G$ with every term in some chief series of $A$. We will also give some applications of our new criterions.