

**Title:** On a variant of the Brocard–Ramanujan equation and an application

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In this paper, we study the variant of the Brocard–Ramanujan diophantine equation  $m! + 1 = u^2$ , where  $u$  is a member of a sequence of positive integers. Under some technical conditions on the sequence, we prove that this equation has at most finitely many solutions in positive integers  $m$  and  $u$ . As an application, we completely solve this equation when  $u$  is a Tripell number. The Tripell numbers are defined by the recurrence relation  $T_n = 2T_{n-1} + T_{n-2} + T_{n-3}$  for  $n \geq 3$ , with  $T_0 = 0$ ,  $T_1 = 1$  and  $T_2 = 2$  as initial conditions.

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