

### Periodicity in radix systems with base 3

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*Dedicated to Professor Imre Kátai for his 85<sup>th</sup> birthday*

**Abstract.** In this paper, we examine the base 3 number expansions in the ring of integers with digits  $\{0, a, -b\}$ ,  $a, b \in \mathbb{N}$  and  $a \equiv b \pmod{3}$ . Among others, we show that for arbitrary natural numbers  $n$  and  $k$ , there is a system where  $n$  has a periodic expansion with length  $k$ . We specify an infinite number of radix systems for a given valid signature.

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