

## What does Birkhoff–James orthogonality know about the norm?

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**Abstract.** It is shown that Birkhoff–James orthogonality knows everything about the smooth norms in reflexive Banach spaces and can also compute the dimensions of the underlying normed spaces.

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