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Characterizing locally polynomial functions on convex subsets of linear spaces

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Abstract. We introduce the notion of locally polynomial functions, satisfying a conditional Fréchet equation on convex subsets of linear space. We prove that locally polynomial functions are solutions to some rather general functional equations. Using Roman Ger's result, we infer that locally they are the restrictions of polynomial functions defined on the whole space.

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