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**Title:** On the counting function of Stanley sequences

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For a finite sequence  $A = \{a_1 < a_2 < \dots < a_t\}$  of nonnegative integers which contains no 3-term arithmetic progression, the Stanley sequence  $S$  generated by  $A$  is defined as follows: for  $k \geq t$ ,  $a_{k+1}$  is the least integer  $a > a_k$  such that  $\{a_1, a_2, \dots, a_k, a\}$  contains no 3-term arithmetic progression. Recently, Moy proved that  $\liminf S(x)/\sqrt{x} \geq \sqrt{2}$ , which solves a problem posed by Erdős et al., where  $S(x)$  is the counting function of  $S$ . In this note we show that  $\limsup S(x)/\sqrt{x} \geq 1.77$ .

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