

Year: 2014

Vol.: 84

Fasc.: 1-2

**Title:** Lepage forms in Kawaguchi spaces and the Hilbert form

**Author(s):** Demeter Krupka

A well-known construction in geometric mechanics and Riemann -Finsler geometry assigns to a (first order) homogeneous Lagrangian the Hilbert form, serving as an integrand in the corresponding variational functional. Analogous constructions, needed for higher-order mechanics and Finsler-Kawaguchi geometry, have not been found yet. In this paper we construct Lepage equivalents of Lagrangians, satisfying higher-order homogeneity (Zermelo) condition. We show that the homogeneity determines uniquely higher-order momenta and annihilates local Hamiltonians. The resulting Lepage equivalents then represent higher-order generalizations of the Hilbert form. This result extends geometric foundations of variational theory to higher-order parameter-invariant variational functionals.

**Address:**

Demeter Krupka  
Lepage Research Institute  
783 42 Slatinice  
Czech Republic  
and  
School of Mathematics  
Beijing Institute of Technology  
5 South Zhongguancun Street  
Haidian Zone, Beijing 100081  
China  
and  
Department of Mathematics  
The University of Ostrava  
70103 Ostrava  
Czech Republic