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Title: Generalization of Wolstenholme's and Morley's congruences

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In this paper, we show that for any prime $p \geq 11$ and any p-integer α, we have $\binom{\alpha p-1}{p-1} \equiv 1-\alpha(\alpha-1)(\alpha^2-\alpha-1)p\sum_{k=1}^{p-1}\frac{1}{k}+\alpha^2(\alpha-1)^2p^2\sum_{1\leq i<j\leq p-1}\frac{1}{ij} \pmod{p^7}$. This congruence generalizes the congruences of Wolstenholme, Morley, Glaisher, Carlitz, McIntosh, Tauraso and Meštrović. Furthermore, it allows to rediscover the congruences of Glaisher, Carlitz and Zhao in a simple way.

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