Year: 2019 | Vol.: 95 | Fasc.: 1-2

Title: Mean invariance identity

Author(s): Janusz Matkowski

For a continuous and increasing function f in a real interval I, and a bivariable mean P defined in I^2 , we prescribe a pair of bivariable means M and N such that the quasiarithmetic mean A_f generated by f is invariant with respect to the mean-type mapping (M, N). This allows to find effectively the limit of the iterates of the meantype mapping (M, N). The means M and N are equal iff P is the arithmetic mean A; they are symmetric iff so so is P. Treating f and P as the parameters, we obtain the family of all pairs of means (M, N) such that the quasiarithmetic mean A_f is invariant with respect to (M, N). In particular, we indicate the function f and the mean P such that the invariance identity $A_f \circ (M, N) = A_f$ coincides with the equality $G \circ (H, A)$, where G and H are the geometric and harmonic means, equivalent to the classical Pythagorean harmony proportion.

Address:

Janusz Matkowski Faculty of Mathematics, Computer Science and Econometrics University of Zielona Góra Szafrana 4A PL 65-516 Zielona Góra Poland