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**Title:** Constrained triangulations, volumes of polytopes, and unit equations

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Given a polytope  $\mathcal{P}$  in  $\mathbb{R}^d$  and a subset  $U$  of its vertices, is there a triangulation of  $\mathcal{P}$  using  $d$ -simplices that all contain  $U$ ? We answer this question by proving an equivalent and easy-to-check combinatorial criterion for the facets of  $\mathcal{P}$ . Our proof relates triangulations of  $\mathcal{P}$  to triangulations of its “shadow”, a projection to a lower-dimensional space determined by  $U$ . In particular, we obtain a formula relating the volume of  $\mathcal{P}$  with the volume of its shadow. This leads to an exact formula for the volume of a polytope arising in the theory of unit equations.

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