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**Title:** Torsion groups of Mordell curves over cubic and sextic fields

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Let  $E$  be a Mordell curve defined over a number field  $K$  by the equation  $y^2 = x^3 + c$ ,  $c \in K$ . Let  $E(L)$  denote the set of  $L$ -rational points of  $E$ , where  $L$  is a number field containing  $K$ . We classify the possible torsion subgroups of  $E(L)$  when  $L$  is a cubic or sextic field, and  $E$  is an elliptic curve over  $L$  or  $\mathbb{Q}$ . We also describe the conditions on  $c$  under which  $E$  has a certain torsion group from the set of all torsion subgroups of  $E(L)$  in the following cases: (i)  $c \in \mathbb{Q}$ ,  $L$  is cubic or sextic; (ii)  $c \in L$ ,  $L$  is cubic.

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