On the intersection of finitely generated free groups. Addendum.

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In a recent note¹) I had given a modified proof of A. G. Howson's result²) that the intersection of two finitely generated subgroups of a free group is itself finitely generated. If the two groups are denoted by U and V, their intersection by W, and their respective ranks by m, n, and N, one has more precisely $N \le 2mn - 2m - n + 1$; under a certain restrictive assumption this could be improved to $N \le 2mn - 2m - 2n + 3$.

I am indebted to Prof. R. BAER for pointing out that in fact this latter result holds without restriction. To see this, one merely has to choose the inner automorphism ξ of the whole free group (cf. the end of $\S 1$, loc. cit.) so that the intersection $W = U \cap V$ is transformed into a group W_1 of nonnegative order $o(W_1)$; the transformed groups U_1 and V_1 will then a fortiori have non-negative orders, that is the first case of $\S 2$, and consequently the improved bound for N, is obtained.

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¹⁾ Publicationes Mathematicae 4 (1956), 186-189.

²⁾ J. London Math. Soc. 29 (1954), 428-434.