

Year: 2022

Vol.: 101

Fasc.: 1-2

Title: Intrinsic metrics under conformal and quasiregular mappings

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The distortion of six different intrinsic metrics and quasi-metrics under conformal and quasiregular mappings is studied in a few simple domains $G \subsetneq \mathbb{R}^n$. The already known inequalities between the hyperbolic metric and these intrinsic metrics for points x, y in the unit ball \mathbb{B}^n are improved by limiting the absolute values of the points x, y , and the new results are then used to study the conformal distortion of the intrinsic metrics. For the triangular ratio metric between two points $x, y \in \mathbb{B}^n$, the conformal distortion is bounded in terms of the hyperbolic midpoint and the hyperbolic distance of x, y . Furthermore, quasiregular and quasiconformal mappings are studied, and new sharp versions of the Schwarz lemma are introduced.

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