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Title: A note on a result of Nathanson

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Let $h \geq 2$ be a positive integer. Let W be a nonempty subset of \mathbb{N} . Denote by $\mathcal{F}^*(W)$ the set of all finite, nonempty subsets of W. Let A(W) be the set of all numbers of the form $\sum_{f \in F} 2^f$, where $F \in \mathcal{F}^*(W)$. Is the asymptotic basis $A = \bigcup_{i=1}^h A(W_i)$

minimal for any partition $\mathbb{N} = W_1 \cup \ldots \cup W_h$? Nathanson [Minimal bases and powers of 2, Acta Arith. **49** (1988), 525–532] showed that this is false for h = 2. In this paper, we consider this problem for all $h \geq 2$.

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