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**Title:** Characterizations of centrality in  $C^*$ -algebras via local convexity of functions

**Author(s):** Gergő Nagy

In this paper, we give a characterization of central elements in a  $C^*$ -algebra  $\mathcal{A}$  in terms of a local property of maps on  $\mathcal{A}$  given by the functional calculus. We prove that if  $f$  denotes one of the functions  $x \mapsto \exp(x)$ ,  $x \mapsto x^3$  ( $x \in \mathbb{R}$ ), a self-adjoint element  $a \in \mathcal{A}$ , which is also positive in the case where  $f$  is the latter map, is central if and only if  $f$  is locally convex at  $a$ .

**Address:**

Gergő Nagy  
Institute of Mathematics  
University of Debrecen  
P. O. Box 400  
H-4002 Debrecen  
Hungary  
and  
HUN-REN-UD Equations, Functions, Curves  
and their Applications Research Group