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Completely bounded approximation property of semigroup crossed products

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Abstract. In this paper, we study the CBAP of the reduced semigroup crossed product $\mathcal{A}\rtimes_{\alpha,r}P$ for a quasi-lattice ordered group (G,P). We prove that if G is amenable and \mathcal{A} has the CBAP, then $\mathcal{A}\rtimes_{\alpha,r}P$ has the CBAP with the same Haagerup constant. We relate the CBAP of $\mathcal{A}\rtimes_{\alpha,r}P$ with an approximation property for completely bounded kernels over P. When P is right Ore, we introduce and characterise the weak amenability of P as the CBAP of the reduced semigroup C^* -algebra with respect to the canonical tracial state and the linear space of finitely supported functions on $P\times P$.

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