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The size of the class 2 residual in finite groups

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Abstract. Let G^c be the class 2 residual of a finite group G. In this paper, it is proved that $|G:Z(G)|<|G^c|^2$ if G is a finite non-abelian group with $\Phi(G)=1$.

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