Publ. Math. Debrecen 107/1-2 (2025), 215–236 DOI: 10.5486/PMD.2025.10171

## Effective weak universality in short intervals

By NITHI RUNGTANAPIROM (Bangkok), JÖRN STEUDING (Würzburg) and SAEREE WANANIYAKUL (Bangkok)

**Abstract.** We prove an effective multidimensional  $\Omega$ -result of Voronin in short intervals [T,T+H] with  $T^{\frac{27}{82}} \leq H \leq T$ , and derive an effective weak universality theorem of the Riemann zeta-function. Furthermore, we provide a few remarks for these results under the assumption of the Riemann hypothesis.

NITHI RUNGTANAPIROM & SAEREE WANANIYAKUL
DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE
FACULTY OF SCIENCE
CHULALONGKORN UNIVERSITY
10330 BANGKOK
THAILAND

JÖRN STEUDING DEPARTMENT OF MATHEMATICS WÜRZBURG UNIVERSITY EMIL FISCHER-STR. 40 97074 WÜRZBURG GERMANY

Mathematics Subject Classification: 11M06, 11M26, 30E10.

Key words and phrases: Riemann zeta-function, uniform approximation, universality.