

On the Lucas and Lehmer sequences in Dedekind domains

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Abstract. In this paper, we first obtain the strong divisibility property for the Lucas and Lehmer sequences in Dedekind domains, and then establish analogues of Zsigmondy’s theorem and the primitive divisor results for such sequences in function fields.

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