

Title: On continuous solutions of n -th order polynomial-like iterative equations

Author(s): Wenmeng Zhang and Weinian Zhang (Corresponding Author)

Many efforts have been made to present all continuous solutions of the iterative equation $\sum_{i=0}^n \lambda_i f^i(x) = c$ but for general n only the case of $c = 0$ was considered and no nonhyperbolic cases were discussed. In this paper we first prove that all continuous solutions are decided totally by those real characteristic roots, which not only gives a method to lower the order when complex characteristic roots are involved but also partly answers the question raised in Remark 8 in [Aequationes Math. 2004, 67: 80–105]. Then we find all continuous solutions of the equation with $c = 0$ in the case of smallest characteristic root being 1. Furthermore, we prove that in the case of all characteristic roots being 1 the equation with $c \neq 0$ has no continuous real solutions when n is even.

Address:

Wenmeng Zhang
Yangtze Center of Mathematics
and Department of Mathematics
Sichuan University
Chengdu, Sichuan 610064
P.R. China
E-mail: mathzwm@sina.com

Address:

Weinian Zhang (Corresponding Author)
Yangtze Center of Mathematics
and Department of Mathematics
Sichuan University
Chengdu, Sichuan 610064
P.R. China
E-mail: matzwn@126.com or matwnzhang@yahoo.com.cn