

Year: 2018

Vol.: 93

Fasc.: 1-2

Title: A domain containing all zeros of the partial theta function

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We consider the partial theta function, i.e., the sum of the bivariate series $\theta(q, z) := \sum_{j=0}^{\infty} q^{j(j+1)/2} z^j$ for $q \in (-1, 1)$, $z \in \mathbb{C}$. We show that for any value of the parameter $q \in (0, 1)$, all zeros of the function $\theta(q, \cdot)$ belong to the domain $\{\operatorname{Re} z < 0, |\operatorname{Im} z| < 132\} \cup \{\operatorname{Re} z \geq 0, |z| < 18\}$. For $q \in (-1, 0)$, all zeros belong to the strip $\{|\operatorname{Im} z| < 132\}$.

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